#### Delta Flow-Salinity Modeling using Physics-Informed Neural Networks

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# Motivation and Goal

#### Motivation

- Delta operations and control strategies frequently accessed using **flow-salinity** relationships.
- Existing artificial neural networks (ANNs) are only data-driven and do not use flow-salinity relations.
- Apply Physics-informed neural network (PINN) that incorporates flow-salinity relations.
- Goal
  - Demonstrate major improvements in salinity estimation using PINN over a conventional ANN.
    - Neural networks using outflow (input variable) and salinity (target output) data.







# What is PINN<sup>[1,2]</sup>?

- The laws of physics are described by differential equations.
- **Neural network** system for solving differential equations.
  - Inputs as independent variables of the function.
  - Differential equation **embedded** into the loss function of the neural network.
- Train the neural network to minimize the loss function.





[1] Raissi, M.; Perdikaris, P.; Karniadakis, G. E. JCP 2019 [2] Psichogios, D. C; Ungar, L. H. AIChE 1992

# Flow-Salinity Relations: **Advection-Dispersion Equation**

- Flow-salinity relations governed by Advection-Dispersion equation.
  - G-model [3,4]. lacksquare
  - Delta Simulation Model II (DSM2) <sup>[5].</sup>  ${}^{\bullet}$

$$A\frac{\partial S}{\partial t} - Q(x,t)\frac{\partial S}{\partial x} = KA\frac{\partial^2 S}{\partial x^2}, \qquad x \in [x_a, x_b], t \in [t_a, t_b]$$

- A is cross-sectional area
- *K* is longitudinal dispersion coefficient
- Q(x, t) is volumetric flowrate
- S(x, t) is concentration of salt
- x is longitudinal direction (increasing in upstream)
- t is time •

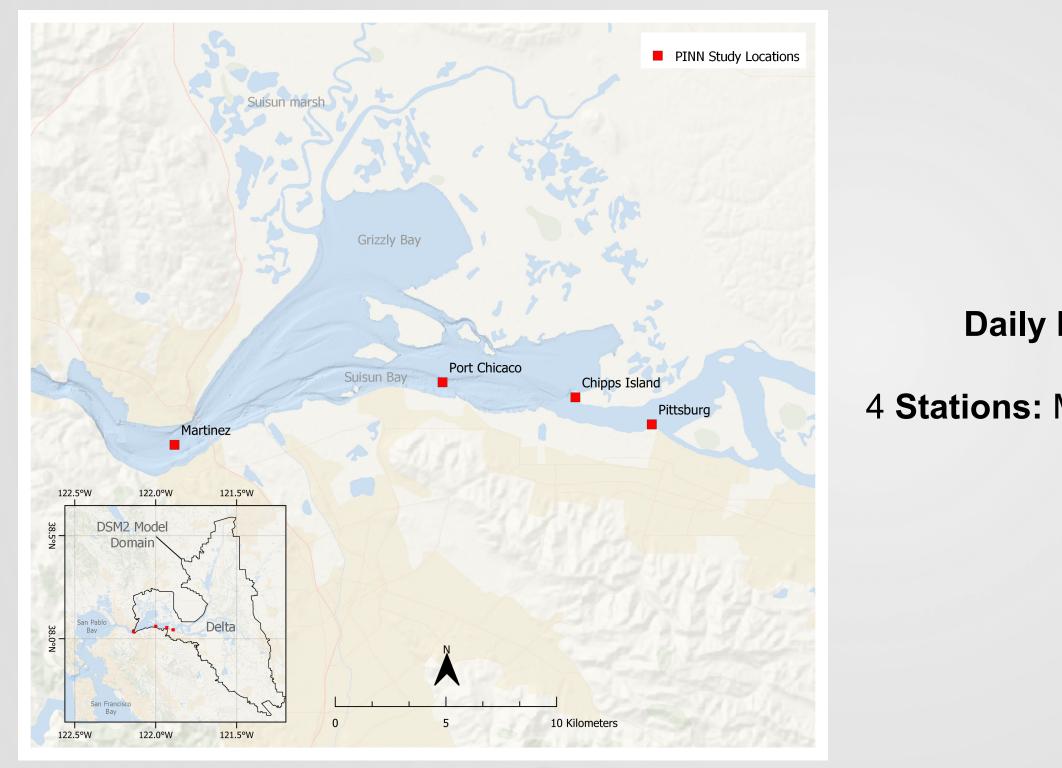






[3] Denton, Richard. ASCE 1993 4/15 [4] Denton, R.; Sullivan, G. CCWD 1993 [5] CDWR. 2019

### **Problem Domain**





WATER RESOURCES



#### Dataset

Daily DSM2 simulated data (outflow and EC) from 1991 to 2015 at 4 Stations: Martinez, Port Chicago, Chipps Island, Pittsburg

## **Outflow Pre-processing**

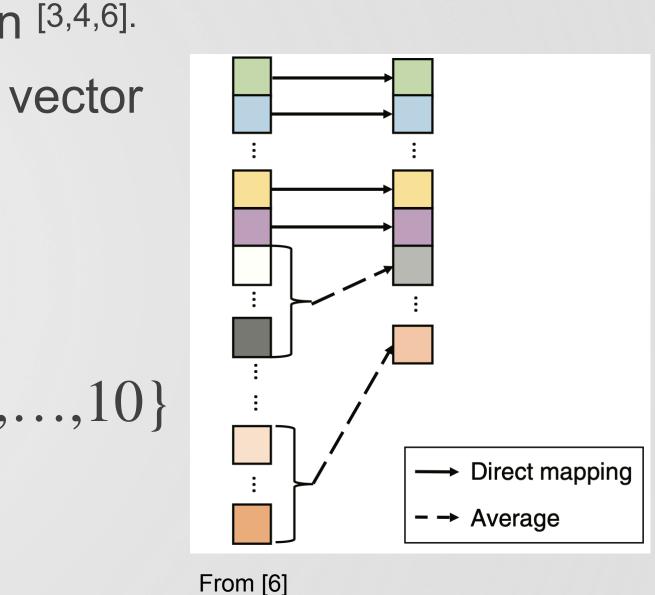
- Important to use antecedent outflow information [3,4,6].
- 118 days of outflow into a 18-dimensional data vector  $\overrightarrow{Q}_n = [Q_{n,1}, ..., Q_{n,18}].$

$$Q_{n,i} = Q_{n-i+1}, \quad \text{for } i \in \{1, \dots, 8\}$$
$$Q_{n,i+8} = \frac{1}{11} \sum_{j=1}^{11} Q_{n-11i-j+4}, \quad \text{for } i \in \{1, \dots, 8\}$$

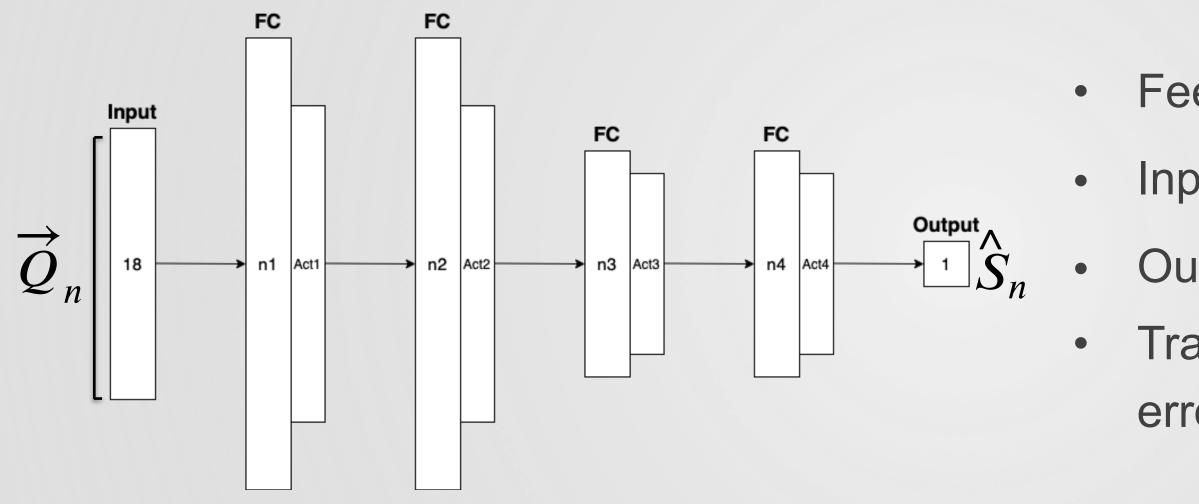




[3] Denton, Richard. ASCE 1993
[4] Denton, R.; Sullivan, G. CCWD 1993
[6] Qi S.; Bai Z.; Ding Z.; Jayasundara N.; He M.; Sandhu P.; Seneviratne S.; Kadir T. JWRPM 2021



### **Conventional ANN**



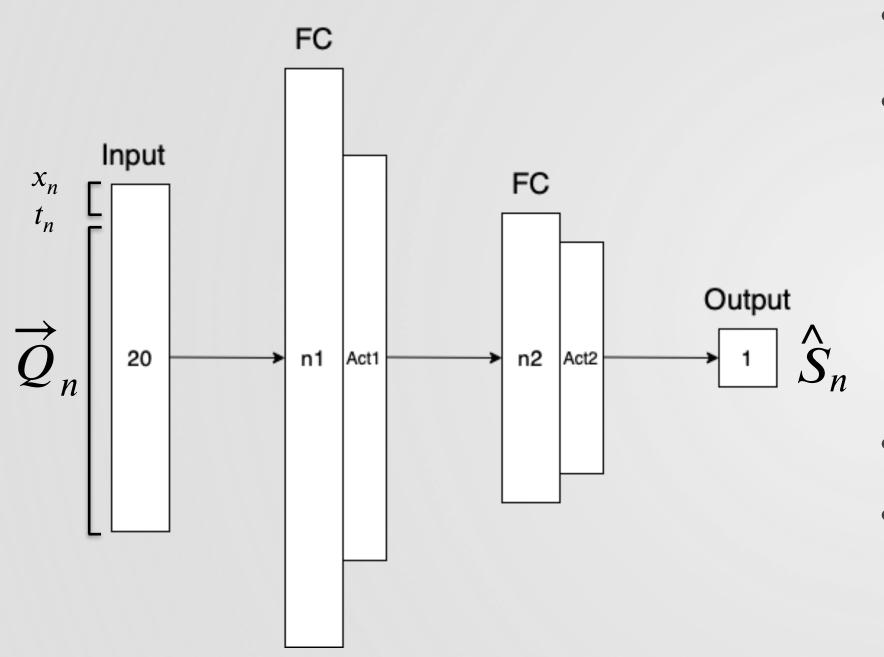




- Feed-forward, fully-connected (MLP)
- Input: outflow data vector  $Q_n$
- Output: estimated EC  $\hat{S}_n$
- Train by minimizing mean square error  $\sum (\hat{S}_n - S_n)^2$

n

# PINN



- Feed-forward, fully-connected (MLP)
- Input: outflow data vector  $\overrightarrow{Q}_n$  and location  $x_n$  and time  $t_n$ 
  - $x_n$  ranging between Martinez and Pittsburg
  - $t_n$  ranging between 1991 and 2015
- Output: estimated EC  $\hat{S}_n$
- Train by minimizing mean squared error and PDE (Advection-Dispersion) loss
  - $\sum_{n} (\hat{S}_{n} S_{n})^{2} + \sum_{n} \left( A \frac{\partial \hat{S}}{\partial t} \Big|_{(x_{n}, t_{n}, \vec{Q}_{n})} Q_{n,1} \frac{\partial \hat{S}}{\partial x} \Big|_{(x_{n}, t_{n}, \vec{Q}_{n})} KA \frac{\partial^{2} \hat{S}}{\partial x^{2}} \Big|_{(x_{n}, t_{n}, \vec{Q}_{n})} \right)^{2}$





# Methodologies

- K-fold cross-validation (5-fold).
- Train: 80% Martinez, Chipps Island, Pittsburg.
- Test: 20% Martinez, Chipps Island, Pittsburg.
- Also test at Port Chicago, an untrained location.
- For each fold: random hyper-parameters search, separately for ANN and PINN.
- Evaluation metrics: Bias, Nash-Sutcliffe Efficiency (NSE),  $r^2$ .
- Inspect salinity time-series.



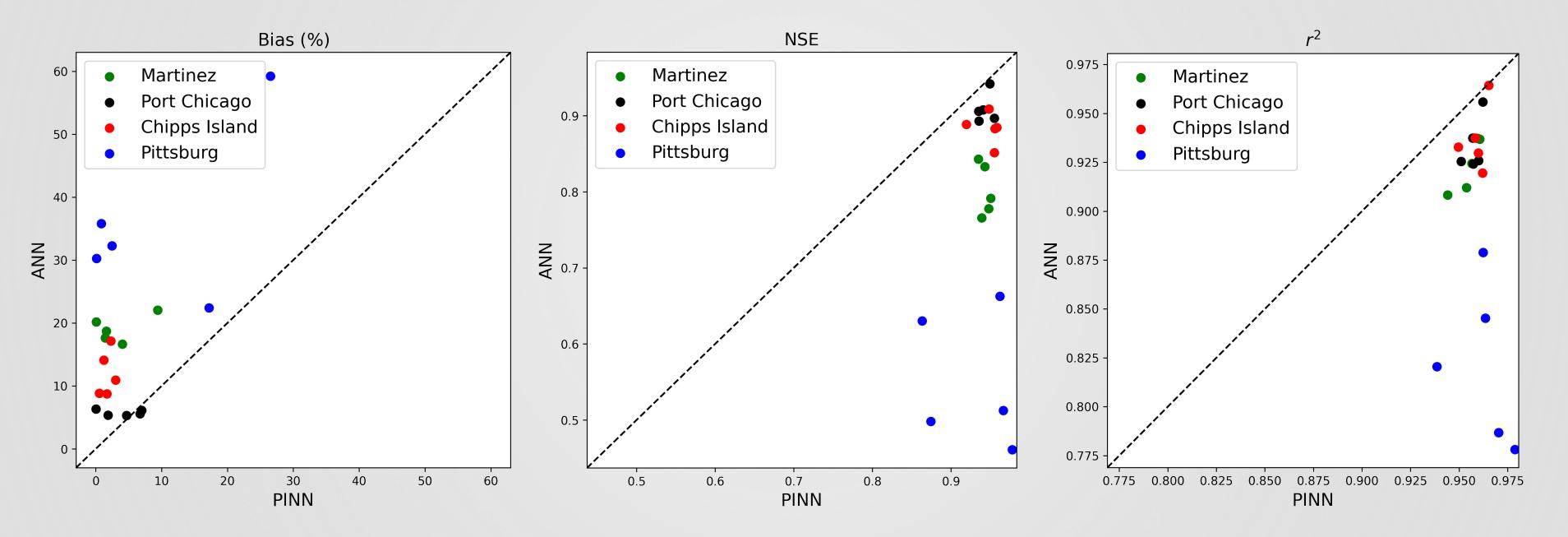






Salinity Data				
19	96 2001	20	06 20	011 201
Test	Train			
Train	Test	Train		
Train		Test	Train	
Train			Test	Train
Train				Test

#### **Results: Scatter Plots**





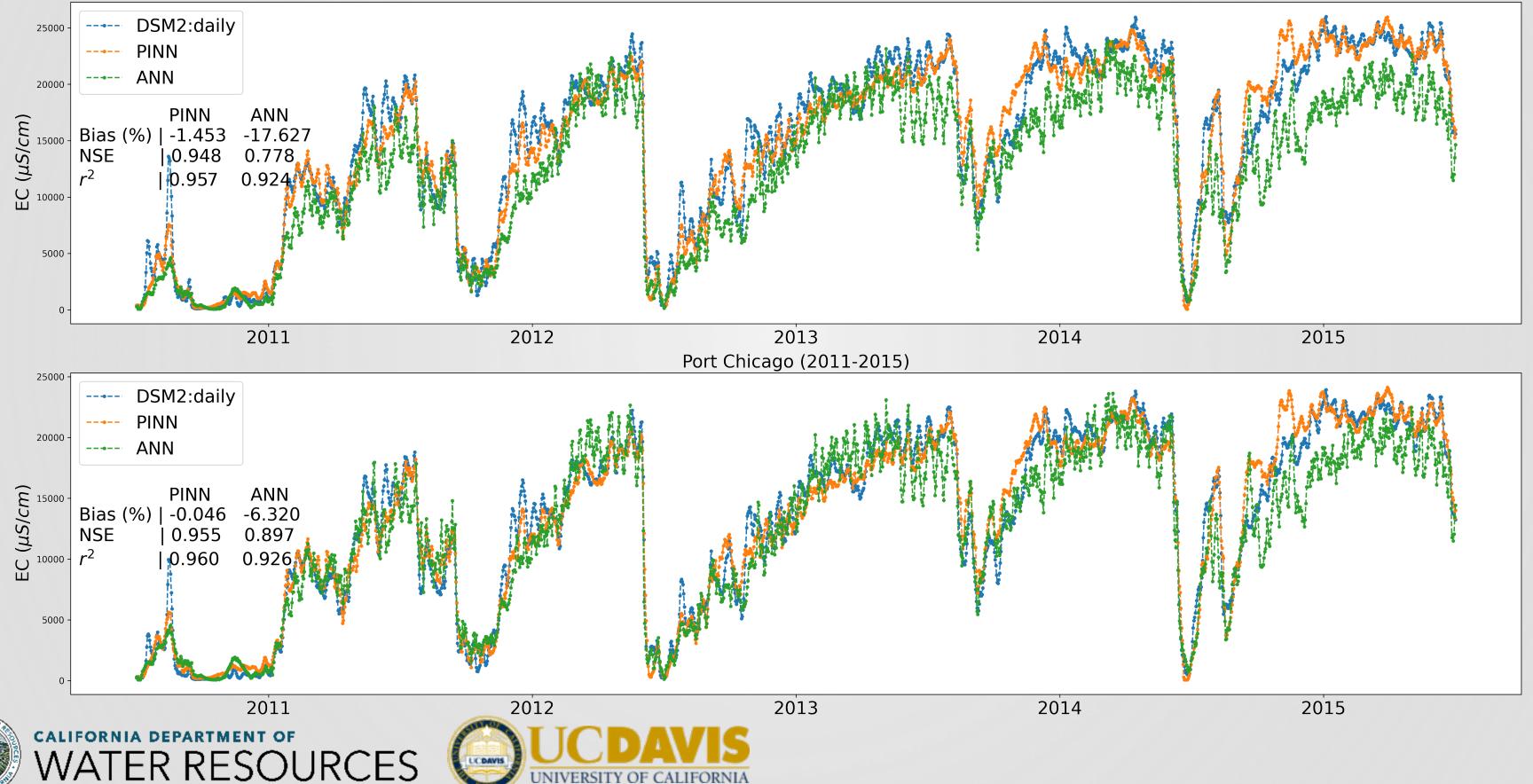


- Smaller Bias
- Larger NSE
- Larger  $r^2$

#### **Greater Performance indicator**

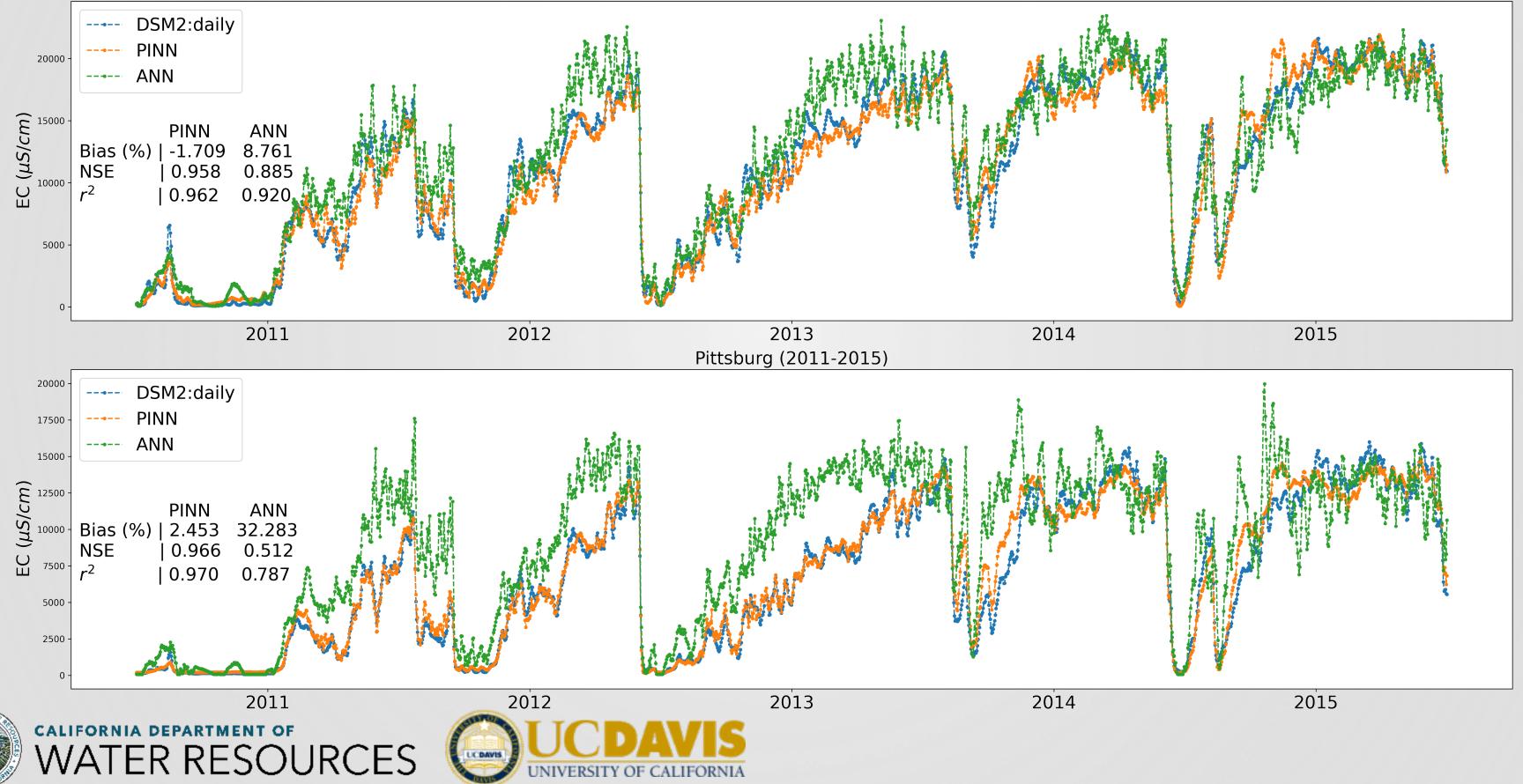
#### **Results: Time-series Plots**

Martinez (2011-2015)



### **Results: Time-series Plots**

Chipps Island (2011-2015)



# Summary and Future Work

#### Summary

- PINN model outperforms ANN model at all four locations.
- Improvement is most significant at Pittsburg, an inner-most location.
- Future Work
  - Further evaluations on more data: other locations, observed data.
  - Varieties of PINN: Fourier Network, LSTM, DGM, etc.  $\bullet$





#### References

[1] Raissi, M., Perdikaris, P., and Karniadakis, G. E. (2019). Physics-informed neural networks: A deep learning framework for solving forward and inverse problems involving nonlinear partial differential equations. Journal of Computational physics, 378:686–707.

[2] Psichogios, D. C. and Ungar, L. H. (1992). A hybrid neural network-first principles approach to process modeling. AIChE Journal, 38(10):1499–1511.

[3] Richard A Denton. Accounting for antecedent conditions in seawater intrusion modeling—
Applications for the San Francisco Bay-Delta. In Hydraulic engineering, pages 448–453. ASCE, 1993.
[4] Denton, R. and Sullivan, G. (1993). Antecedent flow-salinity relations: Application to delta planning

[4] Denton, R. and Sullivan, G. (1993). Antecedent flow-salinity related models. Contra Costa Water District. Concord, California.

[5] CDWR (California Department of Water Resources). 2019. DSM2: Delta simulation model II. Sacramento, CA: Bay Delta Office, CDWR.

[6] Siyu Qi, Zhaojun Bai, Zhi Ding, Nimal Jayasundara, Minxue He, Prabhjot Sandhu, Sanjaya Seneviratne, and Tariq Kadir. Enhanced artificial neural networks for salinity estimation and forecasting in the sacramento-san joaquin delta of california. Journal of Water Resources Planning and Management, 147(10):04021069, 2021.











